

## Shenzhen Workshop on Arithmetic Geometry

Time: March 24-26, 2023.

Organizers: Gao Hui, Hu Yong, Qiu Yannan

Hosted by Dept. of Mathematics at SUSTech.

website: <https://huigaomath.github.io/arithgeom2023.html>

Please note **special time** on Friday.

Time	Mar. 24, Friday	Time	Mar. 25, Saturday	Mar. 26, Sunday
09:00–10:00 <b>(SPECIAL time!)</b>	Zheng Weizhe	09:30–10:30	Xu Daxin	Ren Jinbo
10:00–10:30	Tea break	10:30–10:50	Tea break	Tea break
10:30–11:30	Shen Xu	10:50–11:50	Tian Zhiyu	Luo Caihua
13:00–14:00 <b>(SPECIAL time!)</b>	Cheng Chuangxun	14:00–15:00	Xie Heng	
14:10–15:10	Hui Chunyin	15:00–15:30	Tea break	
15:10–15:30	Tea break	15:30–16:30	Yang Enlin	
		16:40–17:40	Jin Fangzhou	

## I. Title and Abstract.

**Mar. 24, Friday**

**Title:** 平展上同调和超积

**Speaker:** Zheng Weizhe

**Abstract:** 平展上同调的超积提供了代数簇的一族Weil上同调理论，其性质与 $\ell$ 进上同调的 $\ell$ 无关性和无挠性密切相关。本报告将介绍超积上同调研究的新进展。

**Title:** F-zips with additional structure on splitting models of Shimura varieties

**Speaker:** Shen Xu

**Abstract:** We will talk about constructions on certain mod  $p$  Hodge structure for the smooth Pappas-Rapoport splitting models of Shimura varieties. These integral models are resolutions of singularities of the corresponding canonical models for ramified groups. We will also discuss applications to Galois representations associated to torsion classes in coherent cohomology. This is a joint work with Yuqiang Zheng.

**Title:** On the image of Galois representations attached to modular forms

**Speaker:** Cheng Chuangxun

**Abstract:** In this presentation, starting with the results of Swinnerton-Dyer on the congruences of Fourier coefficients of modular forms (small image case) and the results of Serre on the image of Galois representations attached to elliptic curves (big image case), we explain two applications of Galois representations in the study of Fourier coefficients of modular forms.

**Title:** Monodromy of subrepresentations and irreducibility of low degree automorphic Galois representations

**Speaker:**Hui Chunyin

**Abstract:** Given a compatible system  $\{\rho_\lambda : Gal_K \rightarrow GL_n(E_\lambda)\}_\lambda$  of semisimple  $\lambda$ -adic representations of a number field  $K$  satisfying mild local conditions, we prove that for almost all  $\lambda$  any type A irreducible subrepresentation of  $\rho_\lambda \otimes \overline{Q}_\ell$  is residually irreducible. We apply this result and some potential automorphy theorem to prove that  $\rho_\lambda \otimes \overline{Q}_\ell$  is residually irreducible for almost all  $\lambda$  if the compatible system is attached to a regular algebraic, polarized, cuspidal automorphic representation of  $GL_n(A_Q)$  and  $n \leq 6$ .

**Mar. 25, Saturday**

**Title:** Drinfeld Lemma for  $F$ -isocrystals

**Speaker:** Xu Daxin

**Abstract:** Drinfeld's lemma for  $l$ -adic local systems is a fundamental result in arithmetic geometry. It plays an important role in the Langlands correspondence for a reductive group over the function field of a curve over a finite field, pioneered by Drinfeld for  $GL_2$  and subsequently extended by  $L$ . Lafforgue and then  $V$ . Lafforgue. In this talk, we will discuss Drinfeld's lemma for  $p$ -adic local systems: overconvergent/convergent  $F$ -isocrystals. This is based on a joint work with Kiran Kedlaya.

**Title:** Local-global principle, integral Tate conjecture, and algebraic equivalence

**Speaker:** Tian Zhiyu

**Abstract:** I will talk about my recent results about local-global principles for zero cycles and rational points on geometrically rational surfaces defined over global function fields, which is deduced from certain integral version of the Tate conjecture for some classes of varieties over finite fields. The key ingredient is a new geometric understanding of algebraic equivalence of one cycles on smooth projective varieties that has been recently obtained in a joint work with János Kollár.

**Title:**  $I$ -cohomology of Grassmannians

**Speaker:** Xie Heng

**Abstract:**  $I$ -cohomology is a version of the singular cohomology in the real algebraic geometry. It is an important part of the Chow-Witt group, which contains obstruction classes for splitting vector bundles. I will talk about computations about  $I$ -cohomology of Grassmannians.

**Title:** Conductor formulas for motivic spectra

**Speaker:** Yang Enlin

**Abstract:** In this talk, I will begin by making a survey on conductor formulas for constructible étale sheaves. Then I will introduce a quadratic version of Bloch's conductor formula, which is formulated in collaboration with Fangzhou Jin.

**Title:** The quadratic Artin conductor of a motivic spectrum

**Speaker:** Jin Fangzhou

**Abstract:** We define the quadratic Artin conductor of a motivic spectrum over a smooth scheme under some assumptions, and use it to prove a quadratic refinement of the Grothendieck-Ogg-Shafarevich formula. This is a joint work with Enlin Yang.

## Mar. 26, Sunday

**Title:** 丢番图逼近在群论中的应用

**Speaker:** Ren Jinbo

**Abstract:** 一个抽象群 $\Gamma$ 被称为是有界生成的, 如果它可以被写成有限个循环子群的乘积, 即 $\Gamma = \langle g_1 \rangle \cdots \langle g_r \rangle$ 。有界生成在算术群的理论有很多重要应用, 例如Rigidity Property, 同余子群问题, Kazhdan Property (T)等。我们证明, 一个特征零的域上的线性群是能够被半单元素有界生成的当且仅当它是几近阿贝尔 (virtually abelian) 的。特别地, 一个数域上的非迷向的代数群的算术子群一定没有有界生成性质。进一步地, 我们还得出, 一个能够被半单元素有界生成的集合关于高度的增长的速度渐进等于 $c(\log T)^s$ , 其中 $T$ 是高度函数。我们的证明使用丢番图逼近中的子空间定理以及伽罗瓦理论中的generic element理论。这是与Corvaja, Demeio, Rapinchuk和Zannier的合作。

**Title:** Singularity of intertwining operators and some applications

**Speaker:** Luo Caihua

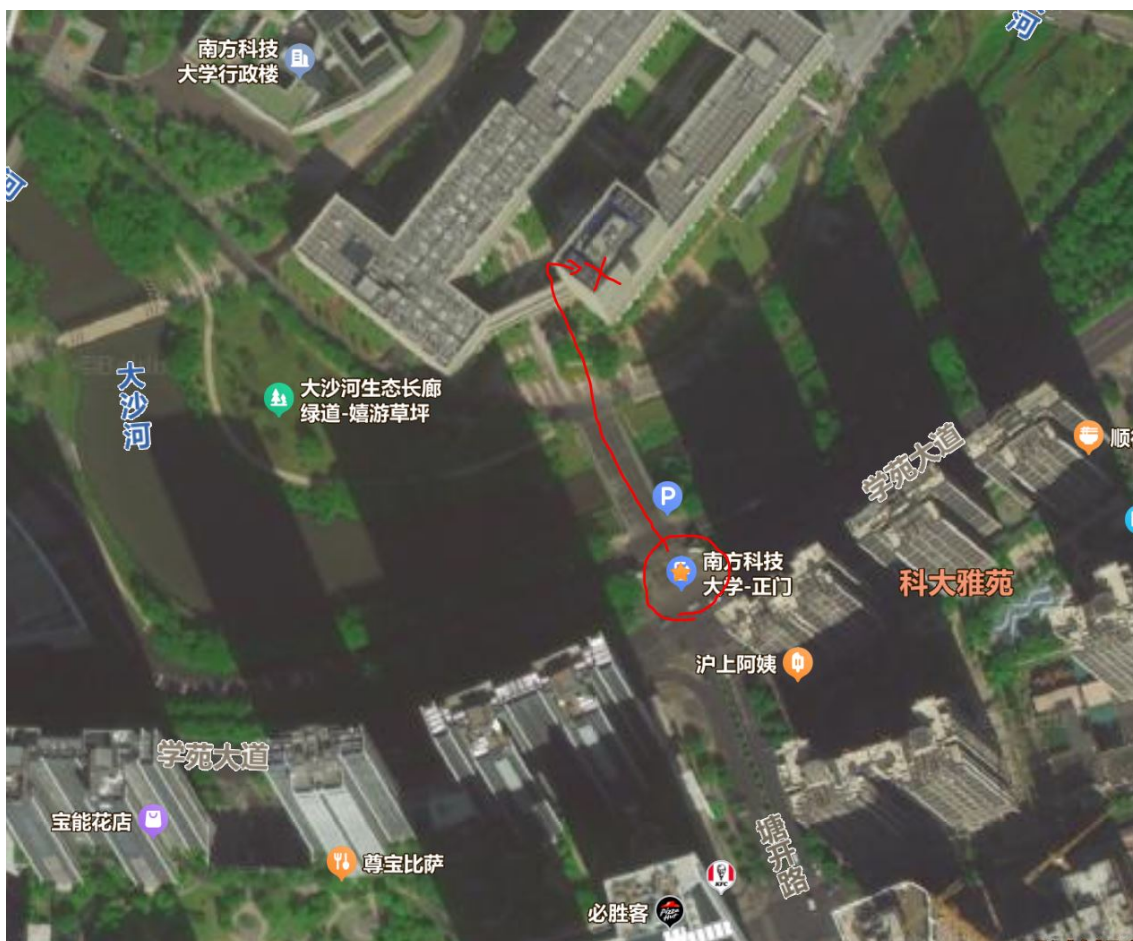
**Abstract:** Intertwining operators play an important role in the Langlands program, e.g. their relations

with constructing automorphic  $L$ -functions. The singularity of those operators is a basic problem. For generic co-rank one generalized principal series, it is characterized by the pole of some Langlands–Shahidi  $L$ -functions. While for generic standard modules, an explicit conjecture was proposed by Casselman–Shahidi about 20 years ago. In this talk, we will present a method to partially answer the singularity problem, especially the aforementioned conjecture. If time permits, we will also discuss some applications.

## II. The Address of the Workshop.

南方科技大学理学院大楼M1001数学系报告厅.

数学系：从1号门，也即图中正门进入。步行100米，图中打叉位置是高的塔楼。1层很容易找到报告厅。



## III. Accommodation information.

维也纳好眠酒店(塘朗地铁站店):

地址:深圳市南山区留仙大道旁

入住方式:报自己姓名,说南科大数学系预订的即可

联系电话:(0755)27776988

雅园塘朗酒店(深圳西丽南科大店):

地址:深圳市南山区学苑大道1133-1号

入住方式:报自己姓名,说南科大数学系预订的即可

联系电话:(0755)22233030

附近公共交通:

地铁 5 号线塘朗站

公交: M369, 43, 74, 81 路, 塘朗小学 (或中科院研究院) 站



## IV. Transportation.

当您到达宝安国际机场或深圳各大火车站、汽车站后，都能通过机场大巴、地铁、公交车、出租车等交通工具前往南方科技大学。推荐乘坐深圳地铁，5号线的塘朗站位于南科大一号门附近。此外，您也可以乘坐出租车来校，目前南方科技大学有四道校园门（一号门、三号门、六号门、七号门）通车。

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**深圳北站:**从深圳北站乘坐地铁与公交来校都十分方便，可乘坐地铁5号线从深圳北站到塘朗站（深圳北站-长岭陂站-塘朗站），并从C出口出站，然后步行700米左右到达学校一号门。

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乘坐地铁11号线到前海湾站，然后换乘地铁5号线到塘朗站并从C出口出站，步行700米左右到达学校1号门。

## V. Map.

